

## 2.4 Examples of application of gene frequencies

When the gene frequencies in a population are known, the genotype frequencies for each genotype under H-W conditions can be calculated. Correspondingly the mating type frequencies under random mating can be calculated by means of the multiplication rule for probabilities, results shown in the table below. Note that when the two genotypes are different, there has to be multiplied with 2, as the two types can be combined in reverse orders.

| Mating type | Frequency                 |                     | Offspring segregation |     |      |
|-------------|---------------------------|---------------------|-----------------------|-----|------|
|             |                           |                     | AA                    | Aa  | aa   |
| AA x AA     | $p^2 \times p^2$          | $= p^4$             | 1                     |     |      |
| AA x Aa     | $2 \times p^2 \times 2pq$ | $= 4p^3 \times q$   | 0.5                   | 0.5 |      |
| Aa x Aa     | $2pq \times 2pq$          | $= 4p^2 \times q^2$ | 0.25                  | 0.5 | 0.25 |
| AA x aa     | $2 \times p^2 \times q^2$ | $= 2p^2 \times q^2$ |                       | 1   |      |
| Aa x aa     | $2 \times 2pq \times q^2$ | $= 4pq^3$           |                       | 0.5 | 0.5  |
| aa x aa     | $q^2 \times q^2$          | $= q^4$             |                       |     | 1    |

Calculation of mating type frequencies is important in relation to control of monogenetic inherited diseases. This topic will be discussed more detailed in chapter 5, where the classical segregation in offspring will be

| Mating type   | Total Freq. | Offspring AA    | Offspring Aa    | Offspring aa      |
|---------------|-------------|-----------------|-----------------|-------------------|
| AAxAA         | 0.9801495   | 0.9801495       | 0               | 0                 |
| AAxAa         | 0.0197014   | 0.0098507       | 0.0098507       | 0                 |
| AaxAa         | 0.0000990   | 0.0000247       | 0.0000495       | 0.0000247 99.00 % |
| AAxaa         | 0.0000495   | 0               | 0.0000495       | 0                 |
| Aaxaa         | 0.0000004   | 0               | 0.0000002       | 0.0000002 0.99 %  |
| aaxaa         | 0.0000000   | 0               | 0               | 0.0000000 0.00 %  |
| Calculate     |             | sum = 0.9900249 | sum = 0.0099500 | sum = 0.0000250   |
| Freq. p 0.995 |             |                 |                 |                   |

Gene frequencies also have a large area of application within bred studies. The gene frequencies for closely related breeds have a tendency to lie closer each other than not so closely related breeds.

**Table 1.** Distribution of albumin types among pure dog breeds and mongrels arranged according to the frequency of the slow allele.

| Breed                          | Genotypes |       |       | Total | Frequency of S |
|--------------------------------|-----------|-------|-------|-------|----------------|
|                                | SS        | SF    | FF    |       |                |
| Basset Hound                   | 0         | 2     | 30    | 32    | 0.03           |
| Beagle                         | 3         | 14    | 52    | 69    | 0.14           |
| Dachshund                      | 2         | 8     | 26    | 36    | 0.17           |
| Small Münsterländer            | 2         | 3     | 12    | 17    | 0.21           |
| Sheepdog, Shetland             | 0         | 6     | 5     | 11    | 0.27           |
| Dalmatian                      | 2         | 3     | 10    | 15    | 0.30           |
| Collie                         | 2         | 21    | 18    | 41    | 0.33           |
| Cocker Spaniel                 | 7         | 24    | 20    | 51    | 0.37           |
| Grey Hound                     | 4         | 6     | 8     | 18    | 0.39           |
| St. Bernhard                   | 3         | 8     | 7     | 18    | 0.39           |
| Labrador Retriever             | 8         | 10    | 10    | 28    | 0.46           |
| German Shepherd                | 36        | 47    | 23    | 106   | 0.56           |
| Old Danish Pointer             | 5         | 5     | 2     | 12    | 0.63           |
| Terrier, Tibetanian            | 10        | 11    | 3     | 24    | 0.64           |
| Terrier, Airedale              | 5         | 12    | 0     | 17    | 0.65           |
| Poodle, Miniature              | 9         | 8     | 2     | 19    | 0.68           |
| Newfoundland                   | 25        | 33    | 3     | 61    | 0.68           |
| Poodle                         | 39        | 36    | 6     | 81    | 0.70           |
| Boxer                          | 54        | 14    | 1     | 69    | 0.88           |
| Carelian Bear Dog              | 15        | 4     | 0     | 19    | 0.89           |
| Golden Retriever               | 53        | 3     | 1     | 57    | 0.96           |
| Great Dane                     | 9         | 0     | 0     | 9     | 1.00           |
| Rottweiler                     | 10        | 0     | 0     | 10    | 1.00           |
| Basenji                        | 44        | 0     | 0     | 44    | 1.00           |
| Other pure breeds              | 94        | 57    | 38    | 189   | 0.65           |
| Mongrels                       | 22        | 41    | 24    | 87    | 0.49           |
| Total                          | 463       | 376   | 301   | 1140  |                |
| Genotypic frequencies          | 0.406     | 0.330 | 0.264 |       |                |
| Expected genotypic frequencies | 0.326     | 0.490 | 0.184 |       |                |

The calculated gene frequencies were  $p(S) = 0.571$

The above shown table gives the results from a study of the albumin types in Danish dog breeds. As mentioned in section 2.1 a fast and a slow albumin allele occur when serum is tested on an electrophoresis gel. These alleles have the designations F and S. The frequencies of the S allele varies from 0 to 1 in the dog breeds. The investigations have been carried out by K. et al. 1985; *Hereditas*, 102:219-223.

In the table below are the results from a study of some mikrosatellites in Danish dog breeds, as well as in the red and the blue foxes. Here are results from three loci each with several alleles, being named as the length of the DNA-string being amplified by the primers. The frequencies vary significantly between the dog breeds. The primers which are developed in the dog work equally well in both fox species. This indicates a large degree of genetic homology between dogs and foxes.  $H^e$  gives the information content of the loci. This depends on the percentage of heterozygotes in the population concerned. Genetically the heterozygotic animals are the most informative. In paternity tests or other genetic investigations the homozygotes give very little or no information about which of the parents' alleles an offspring has inherited. The investigations have been carried out by M. Fredholm et al. 1995; *Mammalian Genome*, 6:11-18.

**Table 2. Allele sizes and allele frequencies of canine microsatellites.**

| Microsatellite locus          | Core sequence                                  | Allele | Flat-coated retriever <sup>a</sup> | Dachshund <sup>b</sup> | Arctic fox <sup>c</sup> | Red fox <sup>d</sup> |
|-------------------------------|------------------------------------------------|--------|------------------------------------|------------------------|-------------------------|----------------------|
| <b>CPH1</b>                   | (TGG) <sub>3</sub><br>- TAG(TGG) <sub>11</sub> | 125    |                                    |                        | 1.00                    |                      |
|                               |                                                | 132    |                                    |                        |                         | 0.30                 |
|                               |                                                | 135    |                                    | 0.14                   |                         |                      |
|                               |                                                | 138    |                                    |                        |                         | 0.70                 |
|                               |                                                | 141    | 0.83                               | 0.56                   |                         |                      |
|                               |                                                | 144    | 0.17                               | 0.30                   |                         |                      |
| <b>H<sup>e</sup><br/>CPH2</b> | (AC) <sub>13</sub>                             |        | 0.21                               | 0.56                   | 0.00                    | 0.40                 |
|                               |                                                | 95     | 0.20                               |                        |                         |                      |
|                               |                                                | 97     | 0.36                               | 0.36                   |                         |                      |
|                               |                                                | 99     | 0.20                               | 0.06                   |                         |                      |
|                               |                                                | 103    |                                    | 0.06                   |                         |                      |
|                               |                                                | 107    |                                    | 0.52                   |                         |                      |
| <b>H<sup>e</sup><br/>CPH3</b> | (GA) <sub>2</sub> TA(GA) <sub>17</sub>         | 109    | 0.24                               |                        |                         |                      |
|                               |                                                |        | 0.94                               | 0.47                   |                         |                      |
|                               |                                                | 154    |                                    |                        | 0.15                    | 0.05                 |
|                               |                                                | 158    |                                    |                        | 0.10                    | 0.25                 |
|                               |                                                | 162    | 0.29                               |                        | 0.45                    | 0.30                 |
|                               |                                                | 164    |                                    |                        | 0.15                    | 0.40                 |
|                               |                                                | 166    |                                    |                        | 0.15                    |                      |
|                               |                                                | 168    | 0.09                               | 0.28                   |                         |                      |
|                               |                                                | 172    | 0.02                               | 0.03                   |                         |                      |
|                               |                                                | 174    |                                    | 0.02                   |                         |                      |
|                               |                                                | 176    | 0.32                               | 0.28                   |                         |                      |
|                               |                                                | 178    | 0.20                               | 0.20                   |                         |                      |
|                               |                                                | 180    | 0.02                               | 0.14                   |                         |                      |
|                               |                                                | 182    | 0.08                               | 0.05                   |                         |                      |
| <b>H<sup>e</sup></b>          |                                                |        | 0.67                               | 0.63                   | 0.80                    | 0.90                 |